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Description Fitting multivariate data patterns with local principal curves, including tools for data compression (projection) and measuring goodness-of-fit; with some additional functions for mean shift clustering. See Einbeck, Tutz and Evers (2005) [<doi:10.1007/s11222-005-4073-8>](https://doi.org/10.1007/s11222-005-4073-8) and Ameijeiras-Alonso and Einbeck (2023) [<doi:10.1007/s11634-023-00575-1>](https://doi.org/10.1007/s11634-023-00575-1).

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Contents

LPCM-package *Local principal curve methods*

Description

Fitting multivariate data patterns with local principal curves, including tools for data compression (projection) and measuring goodness-of-fit; with some additional functions for mean shift clustering.

This package implements the techniques introduced in Einbeck, Tutz & Evers (2005), Einbeck, Evers & Powell (2010), Einbeck (2011), Ameijeiras-Alonso and Einbeck (2023).

The main functions to be called by the user are

- [lpc](#page-11-1), for the estimation of the local centers of mass which describe the principal curve;
- [ms](#page-19-1), for calculation of mean shift trajectories and associated clusters.

The package contains also specialized functions for projection and spline fitting ([lpc.project](#page-15-1), [lpc.spline](#page-16-1)), functions for bandwidth selection ([lpc.self.coverage](#page-3-1), [ms.self.coverage](#page-3-1)), goodness of fit assessment ([Rc](#page-26-1), [coverage](#page-3-2)), as well as some methods for generic functions such as [print](#page-0-0) and [plot](#page-0-0).

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Acknowledgements

Contributions (in form of pieces of code, or useful suggestions for improvements) by Jo Dwyer, Mohammad Zayed, and Ben Oakley are gratefully acknowledged.

Author(s)

Jochen Einbeck and Ludger Evers

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References

Einbeck, J., Tutz, G., & Evers, L. (2005): Local principal curves, Statistics and Computing 15, 301-313.

Einbeck, J., Evers, L., & Powell, B. (2010): Data compression and regression through local principal curves and surfaces, International Journal of Neural Systems 20, 177-192.

Einbeck, J. (2011): Bandwidth selection for nonparametric unsupervised learning techniques – a unified approach via self-coverage. Journal of Pattern Recognition Research 6, 175-192.

Ameijeiras-Alonso, J. and Einbeck, J. (2023). A fresh look at mean-shift based modal clustering, Advances in Data Analysis and Classification, [doi:10.1007/s11634023005751.](https://doi.org/10.1007/s11634-023-00575-1)

See Also

pcurve, princurve

calspeedflow *Speed-flow data from California.*

Description

A 'fundamental diagram' with observations of speed and flow recorded from 9th of July 2007, 9am, to 10th of July 2007, 10pm, on Line 5 of the Californian Freeway SR57-N, VDS number 1202263. The data were originally measured in intervals of thirty seconds, and then aggregated over intervals of 5 minutes length.

Usage

```
data(calspeedflow)
```
Format

A data frame with 444 observations on the following 4 variables.

Date a factor with levels 07/09/2007... 07/10/2007.

Timestamp a factor with a timestamps in intervals of five minutes.

Lane5Flow a numeric vector of vehicle flow in vehicles per 5 minutes.

Lane5Speed a numeric vector of vehicle speed in miles per hour.

Source

Retrieved from PeMS.

References

Einbeck, J., and Dwyer, J. (2011). Using principal curves to analyze traffic patterns on freeways. Transportmetrica 7, 229-246.

Examples

```
data(calspeedflow)
plot(calspeedflow[,3:4])
```
coverage *Coverage and self-coverage plots.*

Description

These functions compute coverages and self-coverages, and produce corresponding plots, for any principal curve object. The former may be used as goodness-of-fit measures, and the latter for for bandwidth selection.

Usage

```
coverage.raw(X, vec, tau, weights=1, plot.type="p", print=FALSE,
      label=NULL,...)
coverage(X, vec, taumin=0.02, taumax, gridsize=25, weights=1,
      plot.type="o", print=FALSE,...)
lpc.coverage(object, taumin=0.02, taumax, gridsize=25, quick=TRUE,
      plot.type="o", print=FALSE, ...)
lpc.self.coverage(X, taumin=0.02, taumax=0.5, gridsize=25, x0=1,
     way = "two", scaled=1, weights=1, pen=2, depth=1,
     control=lpc.control(boundary=0, cross=FALSE), quick=TRUE,
     plot.type="o", print=FALSE, ... )
ms.self.coverage(X, taumin=0.02, taumax=0.5, gridsize=25,
       thr=0.001, scaled=1, cluster=FALSE, plot.type="o",
      print=FALSE, ...)
select.self.coverage(self, smin, plot.type="o", plot.segments=NULL)
```
coverage 5 and 5 a

Arguments

Details

The function coverage.raw computes the coverage, i.e. the proportion of data points lying inside a circle or band with radius τ , for a fixed value tau. The whole coverage curve $C(\tau)$ is constructed through function coverage.

Functions coverage.raw and coverage can be used for any object fitted by an unsupervised learning technique (for instance, HS principal curves, or even clustering algorithms), while the functions prefixing with lpc. and ms. can only be used for the corresponding objects. The functions lpc.coverage and ms.coverage are wrappers around coverage which operate directly a fitted object, rather than a data matrix.

Function select.self.coverage extracts suitable bandwidths from the self-coverage curve, and produces a plot. The function is called from within lpc.self.coverage or ms.self.coverage but can also be called directly by the user (for instance, if the graphical output is to be reproduced, or if the minimum coverage smin is to be modified). The component \$select contains the selected candidate bandwidths, in the order of strength of evidence provided by the self-coverage criterion (the best bandwidth comes first, etc.). A plot is produced as a by-product, which symbolizes the best bandwidth by a thick solid line, the second-best by a dashed line, and the third-best by a dotted line. It is recommended to run the self-coverage functions with fixed starting points, as in the examples below, and to scale by the range only.

See Einbeck (2011) for details. Note that the original publication by Einbeck, Tutz, and Evers (2005) uses 'quick' coverage curves.

Value

A list of items, and a plot (unless plot.type=0).

The functions lpc.self.coverage and ms.self.coverage produce an object of class self. The component \$select recommends suitable bandwidths for the use in lpc, in the order of strength of evidence. These correspond to points of strong negative curvature (implemented via second differences) of the self-coverage curve.

Author(s)

J. Einbeck

References

Einbeck, J., Tutz, G., & Evers, L. (2005). Local principal curves. Statistics and Computing 15, 301-313.

Einbeck, J. (2011). Bandwidth selection for mean-shift based unsupervised learning techniques: a unified approach via self-coverage. Journal of Pattern Recognition Research 6, 175-192.

See Also

[lpc](#page-11-1), [ms](#page-19-1)

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Examples

```
data(faithful)
mfit <- ms(faithful)
coverage(mfit$data, mfit$cluster.center, gridsize=16)
f.self <- ms.self.coverage(faithful,gridsize= 50, taumin=0.1, taumax=0.5, plot.type="o")
h <- select.self.coverage(f.self)$select
f.self <- ms.self.coverage(faithful,gridsize= 50, taumin=0.1, taumax=0<br>h <- select.self.coverage(f.self)$select<br>mfit2 <- ms(faithful,h=h[2]) # using `second-best' suggested bandwidth
data(gvessel)
g.self <-lpc.self.coverage(gvessel[,c(2,4,5)], x0=c(35, 1870, 6.3), print=FALSE, plot.type=0)
```

```
h <- select.self.coverage(g.self)$select
g.lfit \leq lpc(gvessel[,c(2,4,5)], h=h[1], x0=c(35, 1870, 6.3))
```

```
lpc.coverage(g.lfit, gridsize=10, print=FALSE)
```
followx *Fit an individual branch of a local principal curve.*

Description

Internal function of package LPCM called by lpc. Do not use!

Usage

```
followx(Xi, x0, h, t0, iter, way, weights, pen = 2,lasteigenvector = 0, rho0 = 0.4, boundary=0.005,
   convergence.at= 0.000001, cross=TRUE)
```
Arguments

Author(s)

JE

References

Einbeck, J., & Zayed, M. (2014). Some asymptotics for localized principal components and curves. Communications in Statistics - Theory and Methods, 43(8), 1736-1749. [doi:10.1080/03610926.2012.673676](https://doi.org/10.1080/03610926.2012.673676)

See Also

[lpc](#page-11-1)

gaia *Gaia data*

Description

(Simulated) spectral decomposition of stellar objects, generated in the framework of the Gaia project.

Usage

data(gaia)

Format

A data frame with 8286 observations on the following 22 variables.

ID ID of the object

metallicity metallicity (abundance); that is proportion of matter other than hydrogen and helium relative to that of the sun.

gravity the surface gravity; that is acceleration due to gravity at the surface of the star.

- temperature the 'effective' temperature (K); that is the temperature of the observable part of the stellar atmosphere.
- band1 photon counts in band 1
- band2 photon counts in band 2
- band3 photon counts in band 3
- band4 photon counts in band 4
- band5 photon counts in band 5

gaia dia 49.913° ary 1.1131° amin'ny soratra desimaly. Ny faritr'i Normaliesa dia 4.0189.
Ny faritr'ora dia GMT+1.

band6 photon counts in band 6 band7 photon counts in band 7 band8 photon counts in band 8 band9 photon counts in band 9 band10 photon counts in band 10 band11 photon counts in band 11 band12 photon counts in band 12 band13 photon counts in band 13 band14 photon counts in band 14 band15 photon counts in band 15 band16 photon counts in band 16

Details

Gaia is an astrophysics mission of the European Space Agency (ESA) which will undertake a detailed survey of over 10^9 stars in our Galaxy and extragalactic objects. An important part of the scientific analysis of these data is the classification of all the objects as well as the estimation of stellar astrophysical parameters (effective stellar temperature, surface gravity, metallicity). This will be done on the basis of high-dimensional spectroscopic and astrometric data such as those ones given here.

More precisely, the spectral data come in form of photon counts ("fluxes") observed in (originally) 96 wavelength intervals ("bands"), see Bailer-Jones (2010) for more details. The data given here are a 16-dimensional subset created by binning/selecting from the 96 bands. The counts given here are standardized, i.e. they are divided by the total number of incoming photons over all filters (in other words, they add up to 1). Note that these data are simulated using computer models. The satellite which will collect the actual data will be launched in 2012.

The 16-d spectral data have been used in Einbeck, Evers and Bailer-Jones (2008) as well as Einbeck, Evers and Powell (2010) in order to predict the stellar temperature.

Source

Coryn Bailer-Jones (MPIA Heidelberg).

References

Bailer-Jones, C.A.L. (2010). The ILIUM forward modelling algorithm for multivariate parameter estimation and its application to derive stellar parameters from Gaia spectrophotometry, Monthly Notices of the Royal Astronomical Society, vol. 403, pp. 96-116.

Einbeck, J., Evers, L., and Bailer-Jones, C.A.L. (2008). Representing complex data using localized principal components with application to astronomical data. In: Gorban, A, Kegl, B, Wunsch, D, $\&$ Zinovyev, A: Principal Manifolds for Data Visualization and Dimension Reduction; Lecture Notes in Computational Science and Engineering 58, 180-204, ISSN/ISBN: 978-3-540-73749-0.

Einbeck, J., Evers, L., and Powell, B. (2010): Data compression and regression through local principal curves and surfaces, International Journal of Neural Systems, 20, 177-192.

Examples

```
data(gaia)
s <- sample(nrow(gaia),200)
library(lattice)
splom(gaia[s,5:20], cex=0.3, pscales=0)
gaia.pc <- princomp(gaia[s,5:20])
temp <- gaia$temperature
tempcol <- (temp[s]- min(temp[s]))/max(temp[s]- min(temp[s]))
library(scatterplot3d)
scatterplot3d(gaia.pc$scores[,c(2,1,3)], pch="+",
     color=rgb(sqrt(tempcol),0,1-sqrt(tempcol)))
     # This is a 3D scatterplot of the first three principal component scores;
     # with higher stellar temperatures shaded in red colour.
```
gvessel *North Atlantic Water Temperature Data.*

Description

These are observations taken over nine days in May 2000 by the German vessel Gauss in the North Atlantic.

Usage

data(gvessel)

Format

A data frame with 643 observations on the following 7 variables.

day2g an integer for the day at which the measurement was taken.

salg a numeric vector with measurements of salinity according to the PSS (Practical Salinity Scale).

tempg a numeric vector with measurements of water temperature in degrees Celsius.

depthg a numeric vector with the water depths (in meters) at which the measurements were taken.

oxyg a numeric vector with measurements of oxygen content (mm per litre of water)

longg longitude

latg latitude

Source

Retrieved by B. Powell from the World Ocean Database.

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References

Einbeck, J., Evers, L., and Powell, B. (2010): Data compression and regression through local principal curves and surfaces, International Journal of Neural Systems, 20, 177-192.

Examples

```
data(gvessel)
pairs(gvessel[,c(3,2,4,5)])
tcol <- (gvessel$tempg- min(gvessel$tempg))/(max(gvessel$tempg)- min(gvessel$tempg))
require(scatterplot3d)
scatterplot3d(gvessel[,2],gvessel[,4],gvessel[,5], color=rgb(tcol,0,1-tcol))
```
kernels.and.distances *Auxiliary kernel and distance functions.*

Description

Internal LPCM functions which are normally not to be called by the user.

Usage

```
\text{kern}(y, x = 0, h = 1)kernd(X, x, h)
kdex(X, x, h)
distancevector(X, y, d = "euclid", na.rm = TRUE)
vecdist(X,Y)
mindist(X,y)
enorm(x)
```
Arguments

Details

kern specifies the base kernel (by default Gaussian) used in lpc ; kernd is the corresponding multivariate product kernel. kdex is a pointwise multivariate kernel density estimator.

distancevector makes use of function vdisseuclid from R package hopach (but that package does not need to be loaded). enorm is the Euclidean norm.

Author(s)

JE

References

Pollard, van der Laan, and Wall (2010). Hierarchical Ordered Partitioning and Collapsing Hybrid (HOPACH). R package hopach version 2.9.1.

lpc *Local principal curves*

Description

This is the main function which computes the actual local principal curve, i.e. a sequence of local centers of mass.

Usage

```
lpc(X, h, t0 = mean(h), x0, way = "two", scaled = 1,weights=1, pen = 2, depth = 1, control=lpc.control())
```
Arguments

Value

A list of items:

Note

All values provided in the output refer to the scaled data, unless scaled=0 or (equivalently) scaled=FALSE. Use [unscale](#page-28-1) to convert the results back to the original data scale.

The default option scaled=1 or scaled=TRUE scales the data by dividing each variable through their range (differing from the scaling through the standard deviation as common e.g. for PCA). The setting scaled=2, and in fact all other settings scaled>0, will scale the data by their standard deviation.

If scaled=1 or if no scaling is applied, then the default bandwidth setting is 10 percent of the data range in each direction. If the data are scaled through the standard deviation, then the default setting is 40 percent of the standard deviation in each direction.

Author(s)

J. Einbeck and L. Evers. See [LPCM-package](#page-1-1) for further acknowledgements.

References

[1] Einbeck, J., Tutz, G., & Evers, L. (2005). Local principal curves. Statistics and Computing 15, 301-313.

[2] Einbeck, J., Tutz, G., & Evers, L. (2005): Exploring Multivariate Data Structures with Local Principal Curves. In: Weihs, C. and Gaul, W. (Eds.): Classification - The Ubiquitous Challenge. Springer, Heidelberg, pages 256-263.

Examples

```
data(calspeedflow)
lpc1 <- lpc(calspeedflow[,3:4])
plot(lpc1)
data(mussels, package="dr")
lpc2 <- lpc(mussels[,-3], x0=as.numeric(mussels[49,-3]),scaled=0)
plot(lpc2, curvecol=2)
data(gaia)
s <- sample(nrow(gaia),200)
gaia.pc <- princomp(gaia[s,5:20])
lpc3 \leftarrow lpc(gaia.pc$scores[, c(2,1,3)], scaled=0)plot(lpc3, curvecol=2, type=c("curve","mass"))
# Simulated letter 'E' with branched LPC
ex<- c(rep(0,40), seq(0,1,length=20), seq(0,1,length=20), seq(0,1,length=20))
ey<- c(seq(0,2,length=40), rep(0,20), rep(1,20), rep(2,20))
sex<-rnorm(100,0,0.01); sey<-rnorm(100,0,0.01)
eex<-rnorm(100,0,0.1); eey<-rnorm(100,0,0.1)
ex1<-ex+sex; ey1<-ey+sey
ex2<-ex+eex; ey2<-ey+eey
e1<-cbind(ex1,ey1); e2<-cbind(ex2,ey2)
lpc.e1 <- lpc(e1, h= c(0.1,0.1), depth=2, scaled=0)
plot(lpc.e1, type=c("curve","mass", "start"))
```
lpc.control *Auxiliary parameters for controlling local principal curves.*

Description

This function bundles parameters controlling mainly the starting-, convergence-, boundary-, and stopping-behaviour of the local principal curve. It will be used only inside the lpc() function argument.

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Usage

Arguments

Value

A list of the nine specified input parameters, which can be read by the control argument of the lpc function.

Author(s)

JE

References

[1] Einbeck, J., Tutz, G. & Evers, L. (2005): Exploring Multivariate Data Structures with Local Principal Curves. In: Weihs, C. and Gaul, W. (Eds.): Classification - The Ubiquitous Challenge. Springer, Heidelberg, pages 256-263.

[2] Einbeck, J. and Zayed, M. (2014). Some asymptotics for localized principal components and curves. Communications in Statistics - Theory and Methods 43, 1736-1749.

Examples

```
data(calspeedflow)
fit1 <- lpc(calspeedflow[, c(3,4)], x0=c(50,60), scaled=1,control=lpc.control(iter=20, boundary=0))
plot(fit1, type=c("curve","start","mass"))
```
lpc.project *Projection onto LPC*

Description

Projects a new observation onto the spline representation of the local principal curve.

Usage

```
lpc.project(object, newdata, ...)
```
Arguments

Value

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Note

The parametrization of the cubic spline function is not exactly the same as that of the original LPC. The reason is that the latter uses Euclidean distances between centers of masses, while the former uses the arc length along the cubic spline. The differences are normally quite small, though.

Author(s)

J. Einbeck and L. Evers

References

Einbeck, J., Evers, L. & Hinchliff, K. (2010): Data compression and regression based on local principal curves. In A. Fink, B. Lausen, W. Seidel, and A. Ultsch (Eds), Advances in Data Analysis, Data Handling, and Business Intelligence, Heidelberg, pp. 701–712, Springer.

See Also

[lpc](#page-11-1), [lpc.spline](#page-16-1)

Examples

```
data(gvessel)
gvessel.lpc <- lpc(gvessel[,c(2,4,5)], scaled=TRUE, h=0.11, x0 = c(35, 1870, 6.3))
lpc.project(gvessel.lpc, newdata=data.frame(salg=35,dephtg= 2000,oxyg=6))
```
lpc.spline *Representing local principal curves through a cubic spline.*

Description

Fits a natural cubic spline component-wise through the series of local centers of mass. This provides a continuous parametrization in terms of arc length distance, which can be used to compute a projection index for the original or new data points.

Usage

```
lpc.spline(lpcobject, optimize = TRUE, compute.Rc=FALSE,
     project=FALSE, ...)
```
Arguments

Details

See reference [2].

Value

Warning

Careful with options project and compute.Rc - they can take rather long if the data set is large!

Note

The parametrization of the cubic spline function is not exactly the same as that of the original LPC. The reason is that the latter uses Euclidean distances between centers of masses, while the former uses the arc length along the cubic spline. However, the differences are normally quite small.

Author(s)

J. Einbeck and L. Evers

References

[1] Einbeck, J., Tutz, G., and Evers, L. (2005). Local principal curves. Statistics and Computing 15, 301-313.

[2] Einbeck, J., Evers, L. & Hinchliff, K. (2010): Data compression and regression based on local principal curves. In A. Fink, B. Lausen, W. Seidel, and A. Ultsch (Eds), Advances in Data Analysis, Data Handling, and Business Intelligence, Heidelberg, pp. 701–712, Springer.

See Also

[lpc](#page-11-1)

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Examples

```
data(gvessel)
gvessel.lpc <- lpc(gvessel[,c(2,4,5)], h=0.11, x0=c(35, 1870, 6.3))
gvessel.spline <- lpc.spline(gvessel.lpc)
plot(gvessel.spline, lwd=2)
```
lpc.spline.auxiliary.functions

Auxiliary functions for spline fitting and projection.

Description

Internal functions of package LPCM called by lpc.spline and others. These will rarely be called directly by the user.

Usage

lpc.splinefun(lpcobject)

lpc.fit.spline(lpcsl, num.knots = 100)

lpc.spline.eval(lpcsl, or.pi, branch = 0)

lpc.project.spline(lpcsl, newdata, num.knots = 100, optimize = TRUE)

```
lpc.curve.length(lpcsl, or.pi, branch = 0, total.subdivisions = 10000,
     min.subdivisions = 100)
```
Arguments

minimum number of subdivisions for arc length computation.

Author(s)

L. Evers and J. Einbeck

See Also

[lpc.spline](#page-16-1)

ms *Mean shift clustering.*

Description

Function for mean shift clustering, which, for a given bandwidth, detects the local modes and performs the clustering.

Usage

```
ms(X, h, subset, thr=0.01, scaled= 1, iter=200, plot=TRUE, ...)
```
Arguments

Details

The methods implemented here can be used for density mode estimation, clustering, and the selection of starting points for the LPC algorithm. They are based on Ameijeiras-Alonso and Einbeck (2023).

It can be shown (Chen, 1995, Comaniciu & Meer, 2002, Li, 2005) that, if the mean shift is computed iteratively, the resulting sequence of local means converges to a mode of the estimated density function. By assigning each data point to the mode to which it has converged, this turns into a clustering technique.

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Value

The function ms produces an object of class ms, with components:

Note

All values provided in the output refer to the scaled data, unless scaled=0 or (equivalently) scaled=FALSE.

The default option scaled=1 or scaled=TRUE scales the data by dividing each variable through their range (differing from the scaling through the standard deviation as common e.g. for PCA). All other settings scaled>0 will scale the data by their standard deviation.

If scaled=1 or if no scaling is applied, then the default bandwidth setting is 5 percent of the data range in each direction. If the data are scaled through the standard deviation, then the default setting is 20 percent of the standard deviation in each direction.

The threshold thr for merging cluster centers works as follows: After identification of a new cluster center, we compute the Euclidean distance of the new center to (each) existing center, relative to the Euclidean distance of the existing center to the overall mean. If this distance falls below thr, then the new center is deemed identical to the old one.

The goodness-of-fit measure Rc can also be applied in this context. For instance, a value of $R_C =$ 0.8 means that, after the clustering, the mean absolute residual length has been reduced by 80% (compared to the distances to the overall mean).

Author(s)

J. Einbeck. See [LPCM-package](#page-1-1) for further acknowledgements.

References

Ameijeiras-Alonso, J. and Einbeck, J. (2023). A fresh look at mean-shift based modal clustering, Advances in Data Analysis and Classification, [doi:10.1007/s11634023005751.](https://doi.org/10.1007/s11634-023-00575-1)

Chen, Y. (1995). Mean Shift, Mode Seeking, and Clustering. IEEE Transactions on Pattern Analysis and Machine Intelligence, 17, 790-799.

Comaniciu, D. and Meer,P. (2002). Mean shift: a robust approach toward feature space analysis, IEEE Transactions on Pattern Analysis and Machine Intelligence 24, 603-619.

Li, X, Hu, Z, and Wu, F. (2007). A note on the convergence of the mean shift, Pattern Recognition 40, 1756 - 1762.

See Also

[ms.rep](#page-21-1), [Rc](#page-26-1), [plot.ms](#page-23-1)

Examples

```
data(faithful)
# Mean shift clustering with default bandwidth (5 percent of data range)
ms(faithful)
```
ms.rep *Mean shift procedures.*

Description

Functions for mean shift, iterative mean shift, and inverse mean shift.

Usage

```
meanshift(X, x, h)
ms.rep(X, x, h, thresh= 0.0001, iter=200)
ms.rep.min(X, x, h, thresh=0.000001, iter=200, adjust.convergence=FALSE, verbose=TRUE)
```
Arguments

Details

The function meanshift computes a single mean shift iteration, and ms.rep computes an iterative series of mean shift iterations. Both of these functions are rarely used on their own, but are typically called by the overarching function [ms](#page-19-1).

The function ms.rep.min implements an inverse version of the mean shift procedure which can be used for the computation of antimodes (minima of the density). The methodology has been presented in the univariate setting in Ameijeiras-Alonso and Einbeck (2023). The function has been tested to a moderate extent in two dimensions, and it can be expected to work here. It has not been tested for higher dimensions. That is, for data of dimension 3 or higher, the function may or may not produce a result which may or may not correspond to an antimode.

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Value

The function meanshift delivers a single (vector-valued) value.

The functions ms.rep and ms.rep.min produce a list with the following items:

Meanshift.points

(called M for ms.rep.min); the trajectory of points found while proceeding from the starting value x to the mode (or antimode, respectively)

Threshold.values

Note

The threshold thresh for stopping mean shift iterations works as follows. At each iteration, we compare the length of the mean shift, that is the Euclidean distance between the point x and its local mean m, to the Euclidean distance between the point x and the overall data mean. If this distance falls below thresh, the mean shift procedure is stopped.

When ms. rep is called by function ms, the relation of the thresholds thr and thresh is thresh = thr^2.

Convergence of the inverse mean shift algorithm is not mathematically guaranteed. Of course, no antimode will be found if there is none (i.e., if the value x is not situated between two modes), in which case the method will return a NA. But the algorithm may also fail to converge if the antimode is associated with a very small density value, which however rarely happens in practice unless the two distributions are fully separated. In this case the inverse mean shift algorithm will oscillate around the antimode. By reducing the step length successively once that such a situation is identified, convergence can still be ensured algorithmically. This adjustment is activated if the option check.convergence is set equal to TRUE. This functionality is experimental, and details are to be reported elsewhere.

Author(s)

J. Einbeck. See [LPCM-package](#page-1-1) for further acknowledgements.

References

Ameijeiras-Alonso, J. and Einbeck, J. (2023). A fresh look at mean-shift based modal clustering. Advances in Data Analysis and Classification, [doi:10.1007/s11634023005751.](https://doi.org/10.1007/s11634-023-00575-1)

See Also

[ms](#page-19-1)

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Examples

```
data(stamps, package="multimode")
h0 < -0.005hist(stamps, breaks=20)
# Take arbitrary starting value x=0.08, sitting between a mode and antimode
mode <- ms.rep(stamps, 0.08,h0)$final
antimode <- ms.rep.min(stamps, 0.08,h0, verbose=FALSE)$final
segments(mode, 0, mode, 100, col=2, lwd=3)
segments(antimode, 0, antimode,100, col=3, lwd=3)
```
plot.lpc *Plotting local principal curves and mean shift trajectories*

Description

Takes an object of class lpc, lpc.spline or ms. In the case of principal curves, it plots any subset of the following components of the local principal curve: Centers of mass; the curve connecting the local centers of mass; the cubic spline representation of the curve; the projections onto the curve; the starting points. For the mean shift procedure, it produces a plot of mean shift trajectories and cluster centers.

Usage

```
## S3 method for class 'lpc'
plot(x, type, unscale = TRUE, lwd = 1, datacol = "grey60",datpch = 21, masscol = NULL, masspch = 15, curvecol = 1, splinecol = 3,
   projectcol = 4, startcol = NULL, startpch=NULL, ...)
## S3 method for class 'lpc.spline'
plot(x, type, unscale = TRUE, lwd = 1, datacol = "grey60",datpch = 21, masscol = NULL, masspch = 15, curvecol = 1, splinecol = 3,
   projectcol = 4, startcol = NULL, startpch=NULL,...)
## S3 method for class 'ms'
plot(x, unscale=FALSE, lwd=1, datcol="grey70", datpch=21, masscol=NULL,
   masspch=15, curvecol=NULL, ...)
```
Arguments

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Value

A plot of adequate dimensionality (depending on the type of object).

For local principal curves, the minimum supported dimension is $d = 2$, and for the mean shift it is $d = 1$. In either case, the maximum supported dimension is $d = 16$. With increasing dimension d, less plotting options tend to be supported. The nicest plots are obtained for $d = 2$ and $d = 3$.

The most flexible plotting option is masscol. Depending on the length of the specified vector, this will be interpreted differently. If a scalar is provided, the corresponding color will be given to all centers of mass (or cluster centers). For LPCs, if the length of the vector is larger than 1, then this option will assign different colours to different depths, or different branch numbers, or to individual data points, depending on the length. The default setting is assigning colours according to depth, in the order red, blue, black.

Warning

This function computes all missing information (if possible), so computation will take the longer the less informative the given object is, and the more advanced aspects are asked to plot!

Author(s)

JE

References

Ameijeiras-Alonso, J. and Einbeck, J. (2023). A fresh look at mean-shift based modal clustering, Advances in Data Analysis and Classification, [doi:10.1007/s11634023005751.](https://doi.org/10.1007/s11634-023-00575-1)

Einbeck, J., Tutz, G., and Evers, L. (2005). Local principal curves. Statistics and Computing 15, 301-313.

Einbeck, J., Evers, L. & Hinchliff, K. (2010): Data compression and regression based on local principal curves. In A. Fink, B. Lausen, W. Seidel, and A. Ultsch (Eds), Advances in Data Analysis, Data Handling, and Business Intelligence, Heidelberg, pp. 701–712, Springer.

See Also

[lpc](#page-11-1), [lpc.spline](#page-16-1) , [ms](#page-19-1)

Examples

```
data(calspeedflow)
lpc1 <- lpc(calspeedflow[,3:4])
plot(lpc1, type=c("spline","project"), lwd=2)
ms1<- ms(calspeedflow[,3:4], subset=sample.int(444,100), plot=FALSE)
    # starts trajectories from 100 random obs'n
plot(ms1, masscol=1)
plot(ms1, curvecol="grey30")
data(mussels, package="dr")
ms2 <- ms(mussels[,-3], scaled=1, h=0.1, plot=FALSE)
plot(ms2, datpch=20, masspch=24)
```

```
print.lpc Printing output for lpc, lpc.spline, and ms objects
```
Description

Takes an object of class lpc, lpc.spline, ms and displays some standard output.

Usage

```
## S3 method for class 'lpc'
print( x, digits = max(3, getOption("digits") - 3), \dots)
## S3 method for class 'lpc.spline'
print(x, digits = max(3, getOption("digits") - 3), ...)
## S3 method for class 'ms'
print(x, digits = max(3, getOption("digits") - 3), ...)
```
Arguments

Value

Some short text.

Author(s)

JE

See Also

[lpc](#page-11-1), [ms](#page-19-1)

Examples

```
data(calspeedflow)
lpc1 <- lpc(calspeedflow[,3:4])
print(lpc1)
lpc2 <- lpc.spline(lpc1)
print(lpc2)
ms1<- ms(calspeedflow[,3:4], plot=FALSE)
print(ms1)
```
Rc *Measuring goodness-of-fit for principal objects.*

Description

These functions compute the 'coverage coefficient' R_C for local principal curves, local principal points (i.e., kernel density estimates obtained through iterated mean shift), and other principal objects.

Usage

 $Rc(x,...)$

```
## S3 method for class 'lpc'
Rc(x, \ldots)## S3 method for class 'lpc.spline'
Rc(x,...)## S3 method for class 'ms'
Rc(x,...)
```
base.Rc(data, closest.coords, type="curve")

Arguments

Details

Rc computes the coverage coefficient R_C , a quantity which estimates the goodness-of-fit of a fitted principal object. This quantity can be interpreted similar to the coefficient of determination in regression analysis: Values close to 1 indicate a good fit, while values close to 0 indicate a 'bad' fit (corresponding to linear PCA).

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For objects of type lpc, lpc. spline, and ms, S3 methods are available which use the generic function Rc. This, in turn, calls the base function base.Rc, which can also be used manually if the fitted object is of another class. In principle, function base.Rc can be used for assessing goodness-offit of any principal object provided that the coordinates (closest.coords) of the projected data are available. For instance, for HS principal curves fitted via princurve, this information is contained in component \$s, and for a a k-means object, say fitk, this information can be obtained via fitk\$centers[fitk\$cluster,]. Set type="points" in the latter case.

The function Rc attempts to compute all missing information, so computation will take the longer the less informative the given object x is. Note also, Rc looks up the option scaled in the fitted object, and accounts for the scaling automatically. Important: If the data were scaled, then do NOT unscale the results by hand in order to feed the unscaled version into base.Rc, this will give a wrong result.

In terms of methodology, these functions compute R_C directly through the mean reduction of absolute residual length, rather than through the area above the coverage curve.

These functions do currently not account for observation weights, i.e. R_C is computed through the unweighted mean reduction in absolute residual length (even if weights have been used for the curve fitting).

In the clustering context, a value of $R_C = 0.8$ means that, after the clustering, the mean absolute residual length has been reduced by 80% (compared to the distances to the overall mean).

Author(s)

J. Einbeck.

References

Einbeck, Tutz, and Evers (2005). Local principal curves. Statistics and Computing 15, 301-313.

Einbeck (2011). Bandwidth selection for nonparametric unsupervised learning techniques – a unified approach via self-coverage. Journal of Pattern Recognition Research 6, 175-192.

See Also

[lpc.spline](#page-16-1), [ms](#page-19-1), [coverage](#page-3-2).

Examples

```
data(calspeedflow)
lpc1 <- lpc.spline(lpc(calspeedflow[,3:4]), project=TRUE)
Rc(lpc1)
```

```
# is the same as:
base.Rc(lpc1$lpcobject$data, lpc1$closest.coords)
```

```
ms1 <- ms(calspeedflow[,3:4], plot=FALSE)
Rc(ms1)
# is the same as:
base.Rc(ms1$data, ms1$cluster.center[ms1$closest.label,], type="points")
```


Description

unscale takes an object of type lpc, lpc.spline, or ms, which had been fitted using option scaled=TRUE, and transforms the scaled components back to the original data scale.

Usage

```
unscale(x, \ldots)## S3 method for class 'lpc'
unscale(x,...)## S3 method for class 'lpc.spline'
unscale(x,...)
## S3 method for class 'ms'
unscale(x,...)
```
Arguments

Value

A list of relevant items, such as LPC, start, cluster.centers, etc., which gives the unscaled versions of these quantities (some of them may carry the value NULL, if the corresponding information was not available from x).

Author(s)

JE

See Also

[lpc](#page-11-1), [lpc.spline](#page-16-1), [ms](#page-19-1)

Examples

```
data(gvessel)
unscale(lpc(gvessel[,c(2,4,5)], h=0.11, x0=c(35, 1870, 6.3)))
```
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